

Fitting of the current signal of the Pulsed Townsend experiment with the gradient descent algorithm

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The Pulsed Townsend experiment is used for determining the transport coefficients for a swarm of electrons in gases (see e.g., Casey 2021, De Urquijo 2007, Haefliger 2018). These transport coefficients include drift velocity, longitudinal diffusion and the effective ionization coefficient. In general, these transport coefficients are determined by fitting an analytical expression, in which the current signal is expressed in terms of these transport coefficients, to the actual current signal that is measured in the experiment by a nonlinear curve fitting procedure. In the literature, different analytical expressions for the current signal are used by different authors, and the employed nonlinear curve fitting procedures are not always publicly available. For this reason, a systematic study of the fitting of the current signal of the Pulsed Townsend experiment is long overdue, and this work makes first steps in that direction.

In this contribution, we investigate the applicability of the gradient descent algorithm for the fitting of the current signal of the Pulsed Townsend experiment. The gradient descent algorithm is a method for unconstrained mathematical optimization, that is commonly used to train machine learning models including linear regression, logistic regression, neural networks, and support vector machines (see e.g. Bishop 2006). This algorithm minimizes the desired differentiable multivariate function by making repeated steps in the direction opposite to the gradient.

In this contribution, we investigate two different analytical expressions for the current signal from the Pulsed Townsend experiment. We have defined two machine learning models that implement these expressions in the *torch.nn.Module* class from the PyTorch library. PyTorch is an open-source library for machine learning, data science, and artificial intelligence, that has been originally developed by Meta AI (see e.g. Ketkar 2021). The transport coefficients, that are determined from the current signal of the Pulsed Townsend experiment, are included in these models as trainable parameters. The models are trained by employing the *torch.optim.Adam* class, which implements the Adam variant of the gradient descent algorithm (see e.g. Barakat 2021), and by using the data that is generated from the corresponding

analytical expressions, by employing NumPy and SciPy open-source libraries (see e.g. Bressert 2013). Three different learning rates are used for drift velocity, diffusion coefficient, and the effective ionization coefficient, to optimize the convergence of the training algorithm, as these three coefficients have different orders of magnitude. We have observed that excellent convergence is obtained for all four combinations of the two PyTorch models and the two current signals. However, it is important to first estimate the initial guess for the drift velocity from the time at which the current signal is being rapidly reduced, due to the absorption of the electron swarm at the anode.

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